

Problem 26.7

The most general form of the derived capacitance for a parallel plate capacitor in terms of the physical parameters of the cap is:

$$C = \epsilon_d \epsilon_o \frac{A}{d},$$

where ϵ_d is the dielectric constant for the material between the plates (the dielectric constant for air is "1" —note that sometimes the symbol used is κ --I don't like this symbol as it looks like "k," the symbol normally used for the combination of constants $\frac{1}{4\pi\epsilon_o}$), ϵ_o is the permittivity of free space, "A" is the area of one plate and "d" is the distance between the plates. With all of this:

$$C = (1)\epsilon_o \frac{A}{d} = \frac{Q}{V_C}$$
$$\Rightarrow d = \epsilon_o V_C \left(\frac{A}{Q} \right)$$

But

$$\sigma = \frac{Q}{A} \Rightarrow d = \frac{\epsilon_o V_C}{\sigma}$$
$$= \frac{(8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2)(150 \text{ V})}{(3.00 \times 10^{-8} \text{ C}/\text{cm}^2)(10^4 \text{ cm}^2/\text{m}^2)}$$
$$= 4.43 \times 10^{-6} \text{ m}$$